

## Modeling physical properties...

## ... and turbulence

## Two-phase wind tunnel with water injection

Cloud properties	modeled in wind tunnel
Saturated air	relative humidity > 95%
Vertical velocities ~ a few m/s	3 m/s air velocity
Liquid water content (LWC) ~ 0.1-1 g/m³	1 g/m³
Relatively small drop diameters	$d_{\text{mean}} \sim 15 \mu\text{m}$
Number density ~ several hundred/cm³	100-400/cm³

Denomination	Formula	In clouds	In the wind tunnel
Max. size of structures:	$L$	$10^2 \dots 10^3 \text{ m}$	0.55 m
Reynolds number:	$\text{Re} = \frac{v \cdot L}{\nu}$	$10^6 \dots 10^7$	$1.1 \cdot 10^5$
Turbulence length scale:	$l = 0.16 \text{ Re}^{-1/8}$	$10^2 \text{ m}$	0.04 m
Turbulent kinetic energy:	$k = \frac{3}{2} u'^2$	$\sim 1 \text{ m}^2/\text{s}^2$	$0.1 \text{ m}^2/\text{s}^2$
Dissipation rate:	$\varepsilon = c_\mu \frac{k^{3/2}}{l}$	$\sim 10^{-2} \text{ m}^2/\text{s}^3$	$0.14 \text{ m}^2/\text{s}^3$
Kolmogorov length scale:	$\eta = \left( \frac{v^3}{\varepsilon} \right)^{1/4}$	$\sim 10^{-3} \text{ m}$	$4 \cdot 10^{-4} \text{ m}$
Kolmogorov time scale:	$\tau_\eta = \left( \frac{v}{\varepsilon} \right)^{1/2}$	$\sim 10^{-2} \text{ s}$	$10^{-2} \text{ s}$

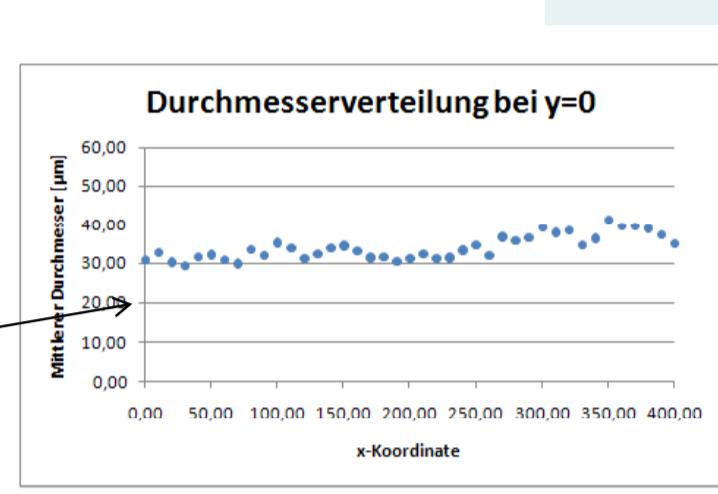
## Concentration / Collisions

Liquid volume fraction ( $\phi = 10^{-6}$ ) is well within the **dilute** domain.  
According to Abrahamson (1975) the collision rate can be defined as:

$$N_c = \frac{1}{2} C^2 d^2 \sqrt{\frac{16 \pi v_p^2}{3}} \approx 2.8 \cdot 10^6 \text{ collisions/s}$$

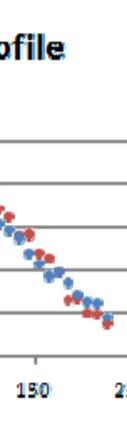
in the measurement section of the wind tunnel (0.45 m x 0.18 m x 0.4 m)

Average residence time in the measurement section:  $\sim 0.15 \text{ s}$   
Average droplet amount in the measurement section:  $7.8 \cdot 10^6$



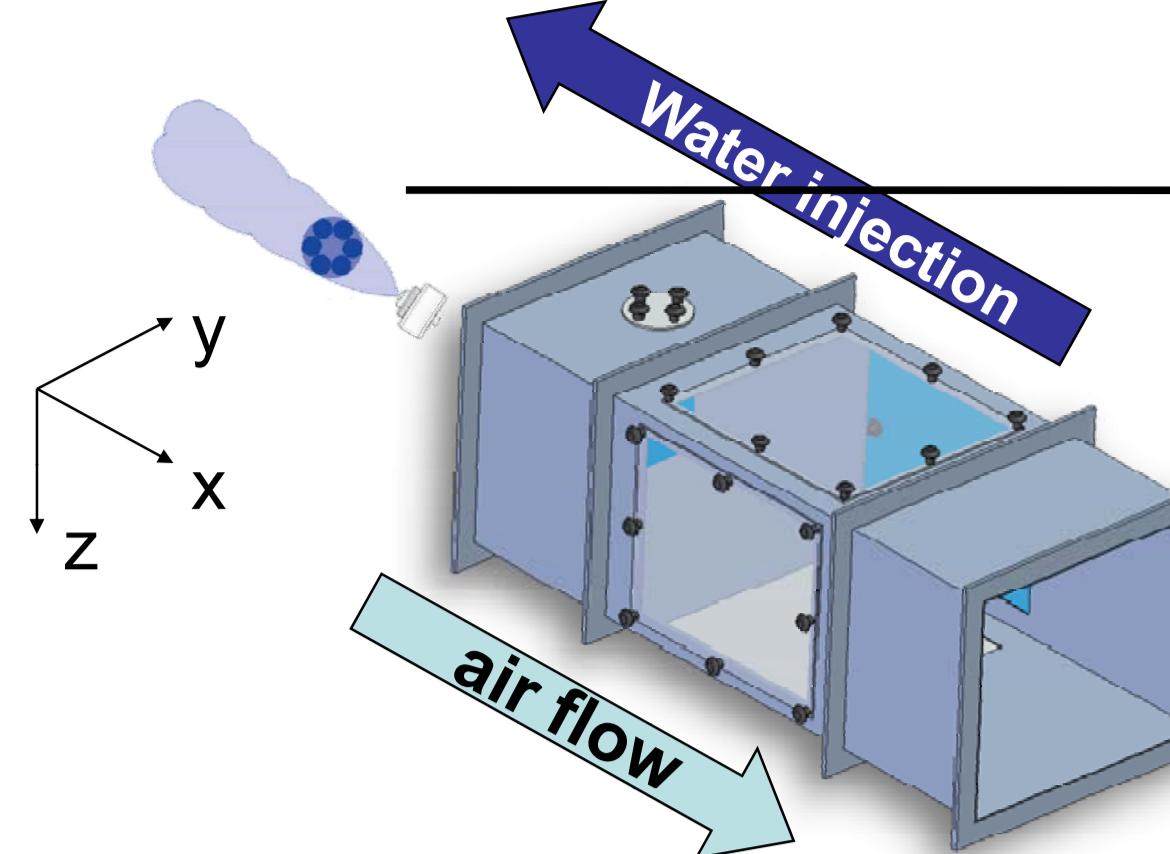
Diameter is increasing with the x-coordinate

Shadowgraphy results can also be used for the concentration calculation besides PDA. Good agreement with the theoretical estimations ☺



AP-E2 (finished): Measuring the configuration M1

Results can be seen here and the data can be found in the look-up table



Final nozzle identified: Lechler 166.208.16.12

Operating parameters:

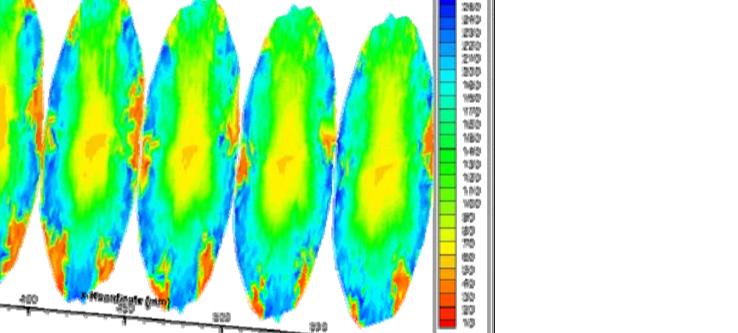
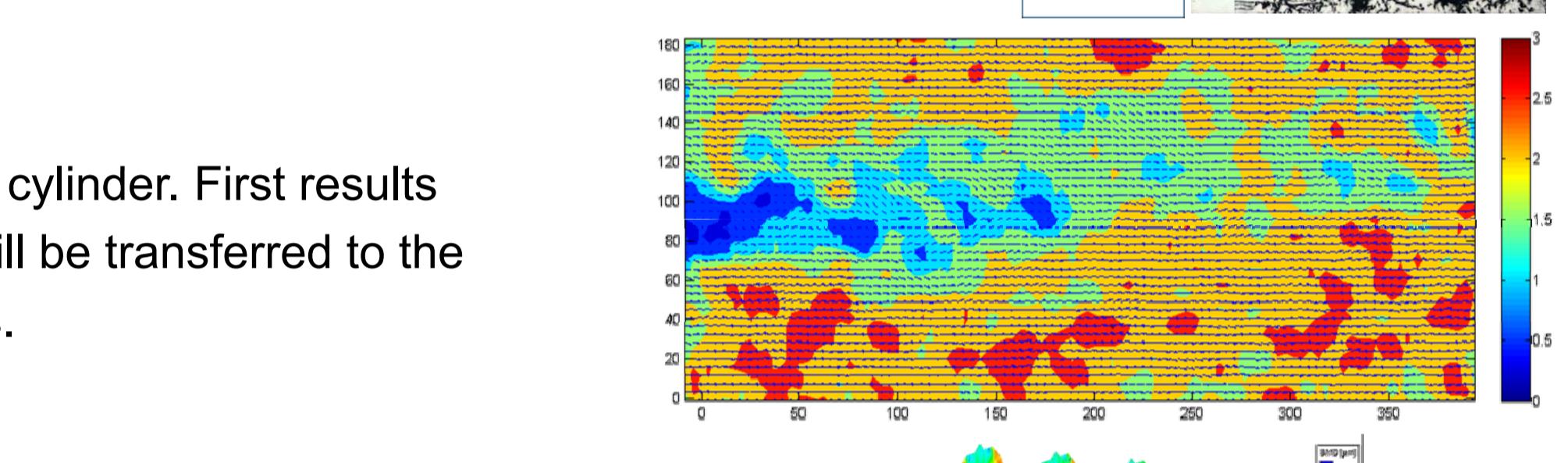
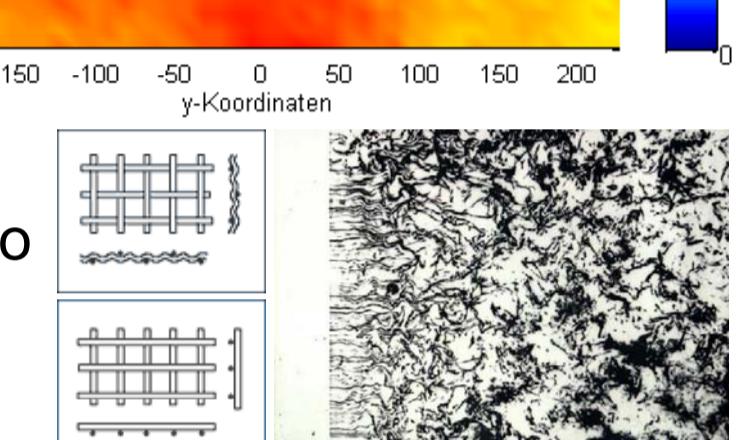
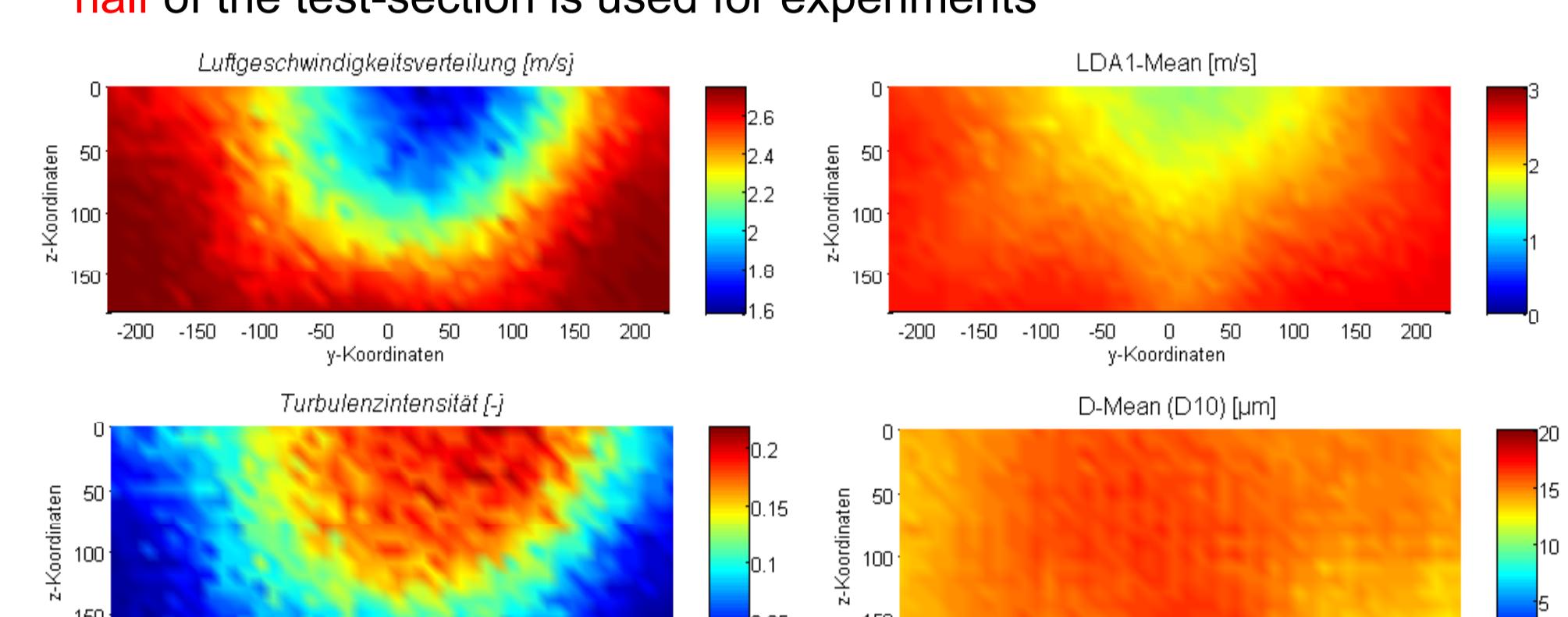
Air pressure: 1.2 bar

Water pressure: 0.9 bar

Volume flow rate: 0.1 l/min

Difficult requirements for the injection:

- Small droplet diameters  $\Rightarrow$  Pressure atomizer
- Broad spray  $\Rightarrow$  nozzle with 60° cone angle
- Low droplet velocities, avoiding 6-hole pattern  $\Rightarrow$  injection in counter-flow direction
- Flow disturbance induced by the nozzle connector  $\Rightarrow$  only the lower half of the test-section is used for experiments



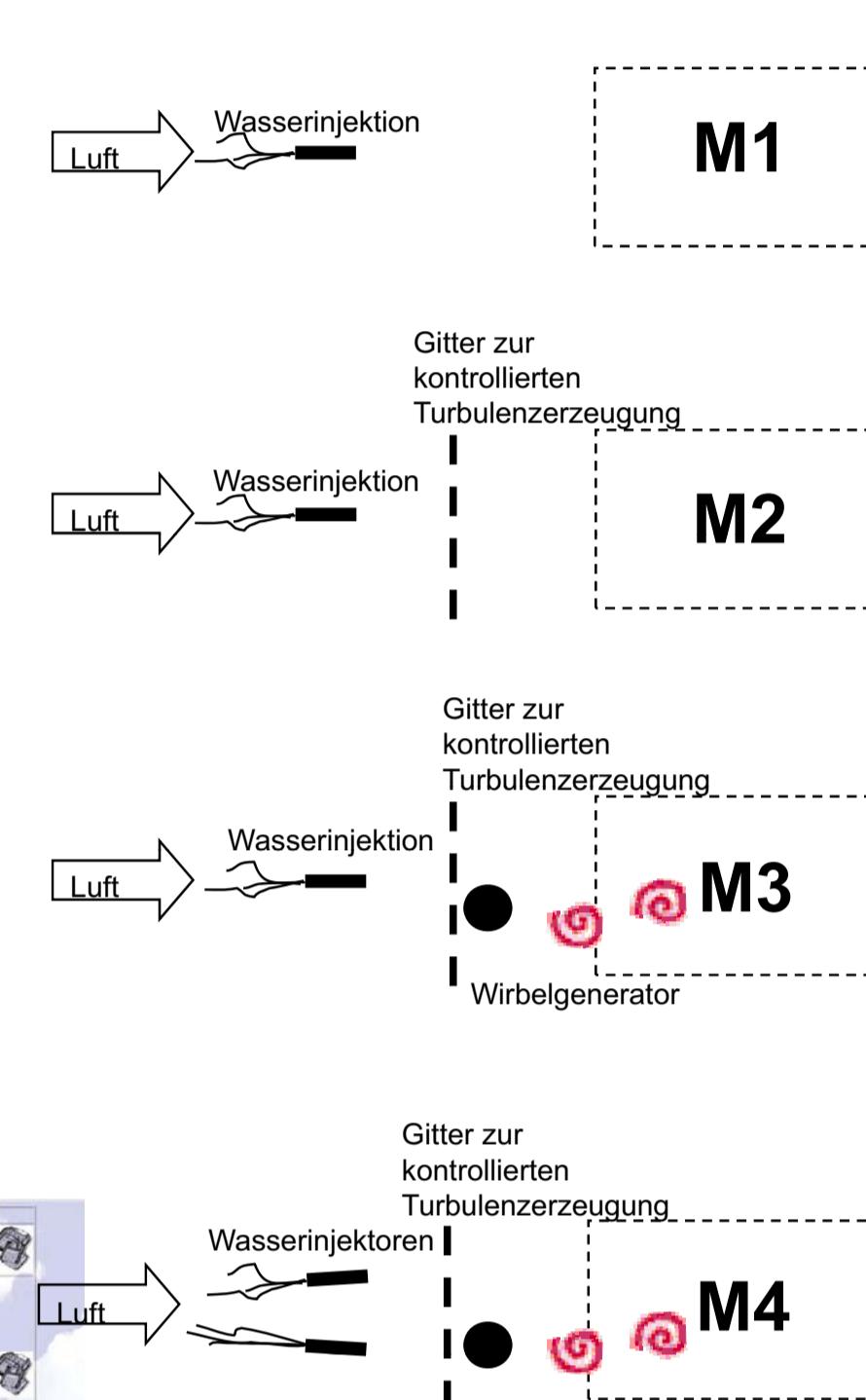
## Configurations and working packages

Method	Phase	Result	$u'$	Remarks
LDV	air	v (point)	+	1-C, high resolution
PDA	drops	v,d (point)	+	1-C, high resolution
PIV	air/drops	v	-	2-C, large meas. area
Shadowgraphy	drops	v,d	-	2-C, collisions
PTV	drops	trajectories	-	3-D, Lagrange

M1	M2	M3	M4
✓	2008/IV	In process	2009/I
✓	2008/IV	In process	2009/I
✓	2008/IV	✓	2009/II
✓	-	-	2009/II

Results into the look-up-table for validation of companion numerical simulations:

[www.ovgu.de/isut/lss/metstroem](http://www.ovgu.de/isut/lss/metstroem)



## AP-E4 (first results):

Measuring the configuration M3  
Vortex generation with the help of a cylinder. First results can be seen here. The final data will be transferred to the look-up table within the next weeks.

## AP-E5 (2009):

Measuring the configuration M4  
Experience with different nozzles available. A suitable nozzle pair has been identified and is available. The droplet spectra have been measured separately.

## REFERENCE EXPERIMENTS IN A MULTIPHASE WIND TUNNEL, NUMERICAL SIMULATION AND VALIDATION

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## Droplet size distribution

• model for ideally mixed fluid, Shaw (2003)

$$\partial_t f(t, r) = J(t, r) - \partial_r(g(t, r)f(t, r)) - \int_0^\infty \kappa(r, r')f(t, r)f(t, r')dr' + \frac{1}{2} \int_0^r \left(1 - \frac{r'^3}{r^3}\right) \kappa\left((r^3 - r'^3)^{\frac{1}{3}}, r'\right) f\left(t, (r^3 - r'^3)^{\frac{1}{3}}\right) f(t, r') dr'$$

-  $r$  – radius of droplets, internal coordinate

-  $f(t, r)$  – droplet size distribution

-  $J(t, r)$  – particle source term, nucleation rate

-  $g(t, r)$  – growth rate; model for sufficiently large droplets and small supersaturations typically given in the atmosphere:  $g(t, r) = \gamma s/r$

-  $\gamma$  – function of environment, like temperature

-  $s$  – supersaturation

• equation is conservation law

change of droplet size distribution  
= (nucleation + growth + collision + coalescence) of droplets

• goals in the first period:

- couple droplet size distribution to flow field

- consider nucleation and growth of droplets

• model system in the first period (dimensionless):

- Navier-Stokes equations

$$\partial_t \mathbf{u} - 2\nabla \cdot (Re^{-1}\mathbb{D}(\mathbf{u})) + (\mathbf{u} \cdot \nabla) \mathbf{u} + \nabla p = \mathbf{0} \quad \text{in } (0, T] \times \Omega, \\ \nabla \cdot \mathbf{u} = 0 \quad \text{in } [0, T] \times \Omega,$$

- transport equation for droplet size distribution

$$\partial_t f(t, \mathbf{x}, r) = J(t, \mathbf{x}, r) - \partial_r(g(t, \mathbf{x}, r)f(t, \mathbf{x}, r)) - \mathbf{u} \cdot \nabla_{\mathbf{x}} f(t, \mathbf{x}, r)$$

in  $(0, T) \times \Omega \times (r_{\min}, r_{\max})$

-  $\Omega$  – wind tunnel

## Numerical simulation of convection-dominated equations with finite element methods

• model problem of transport equation for droplet size distribution: scalar convection-diffusion-reaction equations

$$\frac{\partial u}{\partial t} - \varepsilon \Delta u + \mathbf{b} \cdot \nabla u + cu = 0 \quad \text{in } (0, T] \times \Omega$$

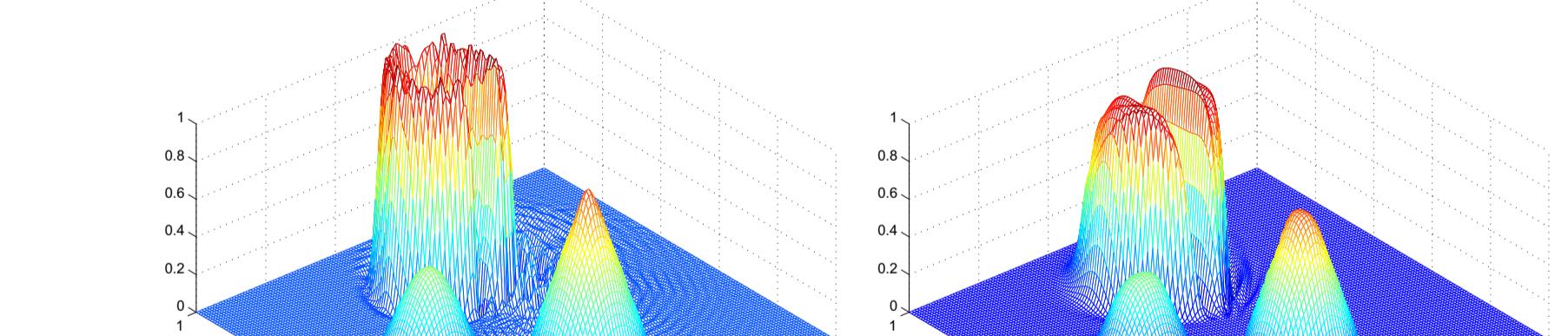
$\varepsilon$  – diffusion,  $\mathbf{b}$  – convection,  $\|\mathbf{b}\| \gg \varepsilon$ ,  $c$  – reaction

- studied finite element methods:

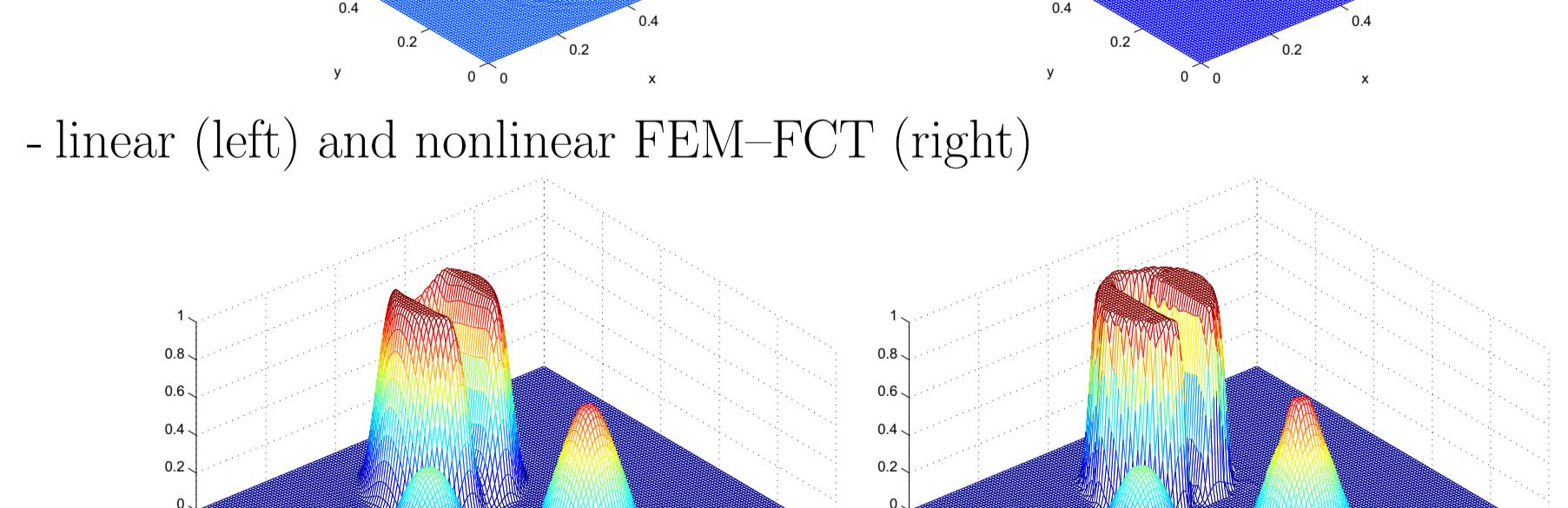
- Streamline-Upwind Petrov-Galerkin (SUPG) FEM (standard method); Hughes, Brooks (1979)
- Spurious Oscillations at Layers Diminishing (SOLD) methods; J., Knoth, Knobloch (2007, 2008)
- Finite Element Methods with Flux Corrected Transport (FEM-FCT); Kuzmin, Möller (2005), Kuzmin (2008)
- Local Projection Stabilization (LPS) scheme; Matthies, Tobiska, Skrzypczak (2007)

- Rotating body problem in 2D

- SUPG (left), SOLD method from Knopp, Lube, Rapin (2006) with  $C = 0.5$  (right)



- linear (left) and nonlinear FEM-FCT (right)



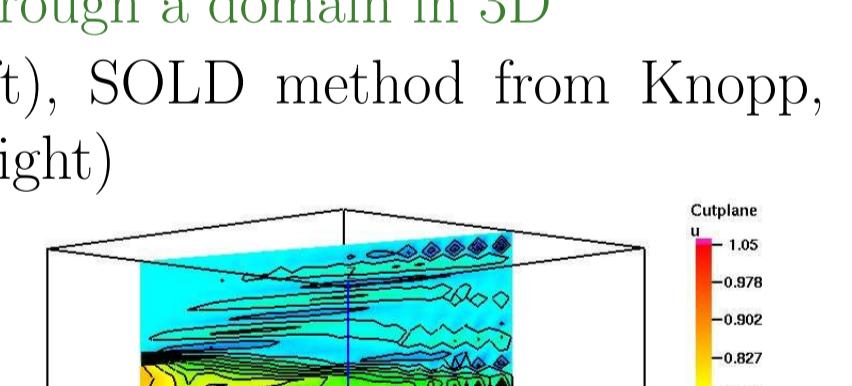
- variation of finite element solutions (optimal value = 1) and computing times in seconds

method	variation	time
SUPG	1.5567	2618
SOLD, $C = 0.1$	1.3990	9501
SOLD, $C = 0.5$	1.2546	22846
SOLD, $C = 1.0$	1.1289	50693
FEM-FCT linear	1.0076	2613
FEM-FCT nonlinear	1.0013	47939

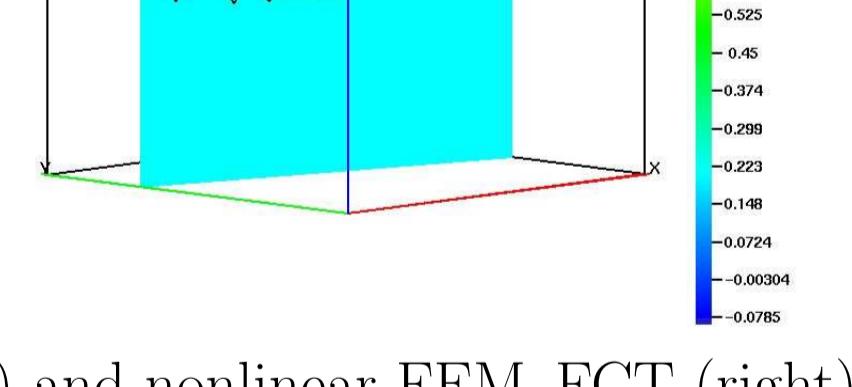
- reference: J., S., Comp. Meth. Appl. Mech. Engrg. (2008), 198, 475 – 494, 2008

- Transport through a domain in 3D

- SUPG (left), SOLD method from Knopp, Lube, Rapin (2006) with  $C = 0.4$  (right)



- linear (left) and nonlinear FEM-FCT (right)



- computing times in seconds

method	$Q_1$	$P_1$
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